Exercise 12

For the following exercises, find the x- or t-intercepts of the polynomial functions.

$$f(x) = x^4 - x^2$$

Solution

To find the x-intercepts, set f(x) = 0 and solve the equation for x.

$$x^{4} - x^{2} = 0$$

$$x^{2}(x^{2} - 1) = 0$$

$$x^{2}(x + 1)(x - 1) = 0$$

$$x^{2} = 0 \text{ or } x + 1 = 0 \text{ or } x - 1 = 0$$

$$x = 0 \text{ or } x = -1 \text{ or } x = 1$$

Therefore, the x-intercepts are (-1,0) and (0,0) and (1,0).

